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**A. Leulmi, S. Leulmi and B. Merikhi**

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**Nazeer Ansari and KH. Herachandra Singh**

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**N. D. Sangle and G. M. Birajdar**

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**George A. Anastassiou**

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**Abstract:** Here are introduced abstract left and right Riemann-Liouville generalized fractional Bochner integral operators of variable order acting over Banach space valued functions. Also are introduced abstract weighted Caputo type left and right fractional derivatives of variable order. Then, we derive abstract left and right fractional integral inequalities of variable orders of Opial, Hardy and Hilbert-Pachpatte types. We give applications to simple Riemann-Liouville fractional integrals of variable order for real valued functions.

**Kushal Roy and Mantu Saha**

SOME RANDOM FIXED POINT THEOREMS FOR PREŠIĆ TYPE CONTRACTIVE  
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371-405

**Abstract:** In the present paper, some deterministic and random fixed point theorems related to several Prešić-type mappings have been investigated. The fixed point theorems proved in this paper due to like Prešić-type mapping are stochastic generalizations of some deterministic fixed point theorems. Moreover, the Ulam-Hyers stability and limit shadowing property of a random fixed point problem have been studied by us. As a consequence, an application has been shown to ensure the existence of random solution of a non-linear stochastic integral equation.

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