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AND THINKER

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Some other related concepts are established as well.

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**Amit Prakash**

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**S. V. Ludkovsky**

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**S. V. Ludkovsky**

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**Arif Rafiq**

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$K : Tx = x$ . Let  $\{\alpha_n\}_{n \geq 0}, \{\beta_n^j\}_{n \geq 0} \in [0, 1], j = 1, 2, \dots, p - 1;$   
 $p \geq 2$  be such that  $\sum_{n \geq 0} \alpha_n^2 = \infty$  and  $\lim_{n \rightarrow \infty} \alpha_n = 0 = \lim_{n \rightarrow \infty} \beta_n^1$ . For  
arbitrary  $x_0 \in K$  let  $\{x_n\}_{n \geq 0}$  be iteratively defined by

$$\begin{aligned} x_{n+1} &= (1 - \alpha_n) x_n + \alpha_n T^n y_n^1, \\ y_n^i &= (1 - \beta_n^i) x_n + \beta_n^i T^n y_n^{i+1}, \\ y_n^{p-1} &= (1 - \beta_n^{p-1}) x_n + \beta_n^{p-1} T^n x_n, \end{aligned}$$

$n \geq 0, i = 1, 2, \dots, p - 2; p \geq 2$ . Then  $\{x_n\}_{n \geq 0}$  converges strongly to  
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