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M. K. Aouf

CERTAIN SUBCLASSES OF MEROMORPHICALLY MULTIVALENT FUNCTIONS ASSOCIATED WITH A CERTAIN LINEAR OPERATOR 1-30

> Abstract: Making use of certain linear operator, we introduce two novel subclasses $Q_n(p, \alpha; A, B)$ and $Q_n^+(p, \alpha; A, B)$ of meromorphically multivalent functions of order α ($0 \le \alpha < p$) in the punctured disc U^* . In this paper we investigate the various important properties and characteristics of these subclasses of meromorphically multivalent functions. We extend the familiar concept of neighborhoods of analytic functions to these subclasses of meromorphically multivalent functions. We also derive many interesting results for the Hadamard products of functions belonging to the class $Q_n^+(p, \alpha; A, B)$.

Rabindra Nath Mondal, Md. Sharif Uddin, Md. Ali Akbar and Bichakshan Mondal

NUMERICAL STUDY OF DEAN VORTICES AND UNSTEADY SOLUTIONS THROUGH A CURVED SQUARE DUCT FLOW 31-56

Abstract: In this paper, flow instability in a curved duct with square cross section is studied numerically by using a spectral method, and covering a wide range of the Dean number $0 \le Dn \le$ 5000 for the curvature $\delta = 0.1$. A temperature difference is applied across the vertical sidewalls for the Grashof number Gr = 100,

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where the outer wall is heated and the inner wall cooled. After a comprehensive survey over the parametric ranges, two branches of asymmetric steady solutions with two- and four-vortex solutions are obtained by the Newton-Raphson iteration method. Linear stability of the steady solutions is then investigated. It is found that only the first branch is linearly stable in a couple of interval of Dn, while the other branch is linearly unstable. Steady values of the Nusselt numbers, Nu, are also calculated for two differentially heated vertical sidewalls. When there is no stable steady solution, time evolutions of Nu as well as their phase spaces are obtained, and it is found that in the unstable region the flow undergoes in the scenario "steady \rightarrow periodic \rightarrow multiperiodic \rightarrow chaotic", if the Dean number is increased.

T. Ram Reddy and R. B. Sharma

A COEFFICIENT INEQUALITY FOR CERTAIN SUBCLASSES OF ANALYTIC FUNCTIONS 57-70

Abstract: The aim of the present paper is to introduce a new subclass of analytic functions of complex order and to obtain the Fekete-Szego inequality for the functions in this class. The Fekete-Szego inequality for the inverse function of f in this class is also obtained. Certain applications of our results for the functions defined through convolution are also obtained.

Deepa Sinha and Pravin Garg

BALANCE AND CONSISTENCY OF TOTAL SIGNED GRAPHS 71-81

Abstract: A signed graph (or sigraph in short) is an ordered pair $S = (S^u, \sigma)$, where S^u is a graph G = (V, E), called the underlying graph of S and $\sigma : E \to \{+, -\}$ is a function from the edge set E of S^u into the set $\{+, -\}$, called the signature (or sign in short) of S. In this paper, first we define *total sigraph* of a given sigraph and then obtain the following theorems:

THEOREM 4. The total sigraph T(S) of a sigraph S is balanced if and only if S is a negatively odd-even sigraph.

THEOREM 13. The total sigraph T(S) of a sigraph S is μ_1 consistent if and only if S is an all-positive sigraph.

M. Alhaz Uddin, M. Abdus Sattar and M. Shamsul Alam

AN APPROXIMATE TECHNIQUE FOR SOLVING STRONGLY NONLINEAR DIFFERENTIAL SYSTEM WITH DAMPING EFFECTS 83-98

> **Abstract:** Based on He's homotopy perturbation technique and the extended Krylov-Bogoliubov-Mitropolskii (KBM) method, an approximate solution is obtained for second order strongly nonlinear ordinary differential system with small damping effects. The method has been illustrated by an example.

Sujoy Chakraborty and Akhil Chandra Paul

On Jordan k-isomorphisms of certain Γ_N -rings 99-111

Abstract: In this paper, we first define k-isomorphism, antik-isomorphism and Jordan k-isomorphism of Nobusawa gamma rings and then develop some useful consequences to prove that every Jordan k-isomorphism of a Nobusawa gamma ring onto a 2torsion free prime Nobusawa gamma ring is either a k-isomorphism or an anti-k-isomorphism. Next we are to show that the similar result is also true if we consider a 2-torsion free prime Nobusawa gamma ring instead of a 2-torsion free prime Nobusawa gamma ring.

Kazuo Kuroki and Shigeyoshi Owa

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> **Abstract:** For the Janowski functions which have been investigated by W. Janowski (Ann. Polon. Math. **23**(1970), 159-177), an extension of some subordinations for the Janowski functions is given, and the Janowski functions defined by some complex parameters are also discussed.

Marcelo F. Farias and Dinamérico P. Pombo Jr.

A UNIVERSAL PROPERTY OF BORNOLOGICAL MODULES AND TOPOLOGICAL MODULES OF MULTILINEAR MAPPINGS 125-161

> **Abstract:** In this work we prove that certain bornological modules of multilinear mappings are isomorphic to bornological projective limits of bornological modules of multilinear mappings and that certain topological modules of multilinear mappings are isomorphic to topological projective limits of topological modules of multilinear mappings.

M. K. Aouf

THE QUASI-HADAMARD PRODUCTS OF CERTAIN ANALYTIC FUNCTIONS WITH NEGATIVE COEFFICIENTS 163-184

> **Abstract:** Two subclasses $T_n^*(p, \alpha, \beta)$ and $C_n(p, \alpha, \beta)$ of certain analytic functions with negative coefficients in the open unit disc are introduced. In this paper, we give some interesting results involving the quasi-Hadamard product of functions belonging to the above subclasses. All of our results are sharp and our results

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are the generalizations of earlier results given by Schild and Silverman [17], Owa [12], Salagean [16] and Patel and Acharya [15], and provide the improvements in the previous results obtained by Owa [13] and Patel and Acharya [15].

Peter Danchev

ON SOME PROPERTIES OF SOCLE-REGULAR AND STRONGLY SOCLE-REGULAR ABELIAN *p*-GROUPS 185-193

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Rui-Xiang Gu, Bin Huang and Hui Huang

On the complex oscillation of a certain differential equation 195-213

Abstract: In this paper, we investigate the growth of solutions of a certain second order homogenous linear differential equation with the form $f'' + (A_1e^{az} + A_2e^{cz})f' + A_0e^{bz}f = 0$ and its nonhomogenous form, we obtain the sharp estimation of the order and the hyper-order of the solutions of the equations which improve the results of Chen, Cheng and Zhou in the references of [5], [6] and [10].